# Lecture 11: Code Review and SIMD Instructions

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• Still working on grading

• Code/slides from today posted after class

• Questions?

## **Assignment 2 Optimizations**

• Lots of cool ideas!

• Some seem very nice but don't speed things up much.

## Assignment 2: Some ideas that seemed to work

- Large base case
  - Why is this good? (Hint: why was Hirshberg's a good idea in the first place?)
  - 300, 2048 both used
  - Both small enough that len1 \* len2 fits in cache
- Iterative version!
  - Recursive calls have overhead; can skip them
  - To be honest this seems like it should be a lower-order term to me
- Don't reverse strings?
  - Just doing the DP backwards might be faster(?)

## Cool ideas that didn't speed things up much

- Using 1 array instead of 2 when calculating the edit distance value
- Getting fancy with calculating the min
  - Two if statements seems fastest
  - I think: compiler is really good at optimizing that.
- Easiest way of passing around solution seemed to be continuously appending each piece as it's found
- Idea: the way the recursive calls work, the solution for the second half is always after the solution for the first half

## Code from best last year (calculating costs)

```
long halflen = len1/2;
for(i=0;i<halflen+1;i++) {</pre>
    long* cur row = table + (i\&2)*(len2+1):
    long* last row = table + ((i+1)%2)*(len2+1);
    cur_row[0] = i;
    for(j=0;j<len2;j++) {</pre>
        //top edge of table
        if (i==0) {
            table[j+1] = j+1;
        } else {
            char c1 = str1[i-1+str1start]:
            char c2 = str2[i+str2start];
            long a = last row[j+1] + 1;
            long b = last_row[j] + (!!(c1^c2));
            long c = cur row[i] + 1;
            long min = (a < b) ? a : b;
            if (c < min) min = c;
            cur row[j+1] = min;
```

## Code from best last year (iterative Hirschberg's)

```
while(stack ptr >= 0) {
     long len1 = stack len1[stack ptr];
     long len2 = stack_len2[stack_ptr];
     long str1start = stack str1start[stack ptr];
     long str2start = stack str2start[stack ptr];
     stack ptr--;
–127 lines: printf("str1: <u>");–––––</u>
     stack ptr++:
     stack len1[stack ptr] = len1-halflen;
     stack str1start[stack ptr] = str1start+halflen;
     stack len2[stack ptr] = len2-min i;
     stack str2start[stack ptr] = str2start+min i;
     stack ptr++;
     stack_len1[stack_ptr] = halflen;
     stack_str1start[stack_ptr] = str1start;
     stack_len2[stack_ptr] = min_i;
     stack str2start[stack ptr] = str2start;
```

## A note on memory usage

- Efficient memory usage depends on *reusing* memory
- (Like the space-efficient ED DP just reused two arrays)
- If using malloc/free to reuse space: need to be careful how you free!
- Making Hirshberg's space-efficient was not meant to be a gotcha question. I'm going to go back and make sure my comments are correct and give back some points.
- Let's go over how this works together.

How much space does this solution require?

Answer: space allocated over whole function, plus max(space used during recursive calls but freed by the end), plus sum(space used during recursive calls and not freed)

Let x, y be size of strings in recursive call.

Allocates O(x + y) space. Maximum space used (and freed) by any recursive call is O(x/2 + y - 1). No space used and not freed by recursive call.

Level  $\ell$  of the recursion uses  $\Omega(n - \ell)$  space. Number of levels is  $\log_2 m$ . Total:  $\Omega(n \log_2 m)$ .

Allocates O(x) space. (No, this is not enough to store a solution; this is just an example.) Maximum space used (and freed) by any recursive call is O(x/2). No space used and not freed by recursive call.

Level  $\ell$  of the recursion uses  $\Omega(m/2^{\ell})$  space. Total space:  $\Omega(m)$ .

Allocates O(x) space. O(x/2) space used and not freed by each recursive call (for O(x) total)

Level  $\ell$  of the recursion uses O(m) space. Total space:  $O(m \log_2 m)$ .

```
hirshbergs(char* tempSolution, char* str1, int len1,
    char* str2, int len2){
  char* solArray1, solArray2;
  hirshbergs(solArray, str1, len1/2, str2, minItem);
  hirshbergs(solArray2, str1 + len1/2, len1 - len1/2,
      str2 + minItem, len2 - minItem);
  tempSolution = malloc(strlen(solArray) +
      strlen(solArray2) + 1);
  tempSolution[0] = ' \setminus 0';
  strcat(tempSolution, solArray);
  strcat(tempSolution, solArray2);
  free(solArrav1);
  free(solArray2); }
```

Only allocate space for each solution character once. Space: O(n + m).

Space: O(n + m).

## **Assignment 2 Question Comments**

- Idea: very similar setup to edit distance
- Need to be careful when gluing the two subproblems together
- In particular: unlike edit distance, need to be careful when reversing the problem
  - First item needs to be on first shelf—but last item doesn't need to be on last shelf

## Hash Functions in Practice

Of course, we want consistency (each time we hash an item we get the same result back). What else might we want?

- Fast
- Low space requirements (i.e. may need to store a seed; don't want that to be too big)
- Good collision avoidance
- Bear in mind: different hashes work on different types of elements. We'll focus on integers and strings (especially strings)

## Ideal Hash Functions (Independent, Uniform Hashing)

- Perfect collision avoidance
- But: require extremely large space usage unless universe of possible elements is extremely small
- You did use one of these...
  - For *h* on Assignment 3! Those values were all chosen independently, completely at random

 Anyone know how Java hashes a 64 bit Long?

return x ^ (x >> 32);

• Advantages of this?

## Is this good for:

- In cuckoo filter:  $h_1$ , h, f?
  - h1 and f: might work if elements are fairly well-spread (we take mod)
  - *h*: probably won't work (output too small)
- CMS? HLL?
  - CMS might be OK; prob not (same as above)
  - HLL likely useless unless elements very uniformly spread

```
uint64_t hash3(uint64_t value){
    return (uint64_t)(value * 0x765a3cc864bd9779) >> (64 -
        SHIFT);
}
```

- Hash from Mini-Midterm 1
- Seed is a large prime number to multiply by; can also add a large random prime
- Advantages?
  - Fast! (And easy.)

```
uint64_t hash3(uint64_t value){
    return (uint64_t)(value * 0x765a3cc864bd9779) >> (64 -
        SHIFT);
}
```

}

- How good is it?
  - Pretty good! For any x, y, Pr(h(x) = h(y)) = 1/n.
  - But unfortunately behavior doesn't extend to larger numbers of elements.
- Let's say we use this for a hash table with chaining (*n* items, *n* chains). What is the expected number of elements we find during a query *q*?

X<sub>i</sub> = 1 if h(x<sub>i</sub>) = h(q). Then E[X<sub>i</sub>] = 1/n. By linearity of expectation, total number of items is ∑<sup>n</sup><sub>i=1</sub> 1/n = 1.

```
uint64_t hash3(uint64_t value){
    return (uint64_t)(value * 0x765a3cc864bd9779) >> (64 -
        SHIFT);
}
```

ſ

- How good is it?
- What is the size of the largest chain?
  - Can't say anything given the above. (If assuming ideal hashes then we'd get  $O(\log n)$ -multiply-shift hashing doesn't guarantee this)
- This hash is fast and good on average, but no concentration bounds on worst-case data.

## Multiply-Shift hashing for other data structures

- Is this going to work well for a filter?
  - Probably not. Would have to try it.
- Count-min sketch?
  - Average performance would work! But concentration bounds may not—the number of rows may not improve performance as much as we'd think
- Hyperloglog?
  - Would have to try but I doubt it.

- Popular practical hash function
- Uses repeated MUltiply and Rotate operations
  - Rotate is like shift, but bits that "fall off" are replaced on other side
  - Can be implemented with two shifts and an OR
- Code isn't exactly short; 50 operations to hash a number

## Murmurhash Code

```
for(i = -nblocks; i; i++)
 uint32_t k1 = getblock(blocks,i*4+0);
 uint32 t k2 = getblock(blocks,i*4+1);
 uint32 t k3 = getblock(blocks,i*4+2);
 uint32_t k4 = getblock(blocks,i*4+3);
 k1 *= c1; k1 = ROTL32(k1,15); k1 *= c2; h1 ^= k1;
 h1 = ROTL32(h1, 19); h1 += h2; h1 = h1*5+0x561ccd1b;
 k_2 = c_2; k_2 = ROTL_{32}(k_2, 16); k_2 = c_3; h_2 = k_2;
 h2 = ROTL32(h2,17); h2 += h3; h2 = h2*5+0x0bcaa747;
 k3 *= c3; k3 = R0TL32(k3,17); k3 *= c4; h3 ^= k3;
 h3 = ROTL32(h3, 15); h3 += h4; h3 = h3*5+0x96cd1c35;
 k4 = c4; k4 = R0TL32(k4, 18); k4 = c1; h4 ^= k4;
 h4 = R0TL32(h4, 13); h4 += h1; h4 = h4*5+0x32ac3b17;
```

## Murmurhash Code

```
switch(len & 15)
```

```
case 15: k4 ^= tail[14] << 16:
case 14: k4 ^= tail[13] << 8;
case 13: k4 ^= tail[12] << 0:
         k4 = c4; k4 = R0TL32(k4.18); k4 = c1; h4 ^= k4;
case 12: k3 ^= tail[11] << 24:
case 11: k3 ^= tail[10] << 16:</pre>
case 10: k3 ^= tail[ 9] << 8;</pre>
case 9: k3 ^= tail[ 8] << 0;</pre>
         k3 *= c3; k3 = ROTL32(k3,17); k3 *= c4; h3 ^= k3;
 12 lines: case 8: k2 ^= tail[ 7] << 24;---
};
h1 ^= len; h2 ^= len; h3 ^= len; h4 ^= len;
h1 += h2; h1 += h3; h1 += h4;
h2 += h1: h3 += h1: h4 += h1:
h1 = fmix32(h1):
h2 = fmix32(h2):
h3 = fmix32(h3):
h4 = fmix32(h4):
h1 += h2; h1 += h3; h1 += h4;
h2 += h1: h3 += h1: h4 += h1:
```

(The light grey lines skip pieces of code.)

## Murmurhash3 Performance

- No known worst-case guarantees (not even Pr(h(x) = h(y)) = O(1/n))
- Someday may discover: might not work well in some circumstances (this is what happened to Murmurhash2)
  - "Will this flaw cause your program to fail? Probably not what this means in real-world terms is that if your keys contain repeated 4-byte values AND they differ only in those repeated values AND the repetitions fall on a 4-byte boundary, then your keys will collide with a probability of about 1 in 2<sup>27.4</sup> instead of 2<sup>32</sup>. Due to the birthday paradox, you should have a better than 50% chance of finding a collision in a group of 13115 bad keys instead of 65536."
  - https://sites.google.com/site/murmurhash/murmurhash2flaw

## Murmurhash3 Performance



Average of square of bucket sizes. Data is an intentionally bad (albeit reasonable) case

From "Practical Hash Functions for Similarity Estimation and Dimensionality Reduction" by Dahlgaard, Knudsen, Thorup NeurIPS 2017

## Murmurhash3 Performance in Practice

- Much more resilient than multiply-shift to more-difficult statistical tests (beyond average case)
- Visual example: let's say we hash "number strings": "1", "2", ... "216553"
- (Cool experiment from https://softwareengineering.stackexchange.com/ questions/49550/which-hashing-algorithm-is-best-for-uniqueness-and-speed)
- (I wouldn't normally cite stackexchange but this is really cool)
- Compare SDBM (another popular hash) with Murmurhash2); fill in pixel if corresponding table entry is hashed to

## SDBM (lots of chunks of full cells!)



## Murmurhash2 (visually: random)



## One last murmurhash question

- Murmurhash really just does a bunch of arbitrary multiplies and rotates
- Is there anything special about this specific sequence, or will any such set work pretty well?
- Answer: others might not work. Example: "SuperFastHash" also uses multiplies and rotates

## Hash comparison

Hash	Lowercase		Random UUID		Numbers	
	======		====			
Murmur	145 n	IS	259	ns	92	ns
	6 c	collis	5	collis	0	collis
SDBM	148 n	IS	484	ns	90	ns
	4 c	collis	6	collis	0	collis
SuperFastHash	164 n	IS	344	ns	118	ns
	85 c	collis	4	collis	18742	collis

SuperFastHash has bad performance on lowercase English words, and horrendous performance on numbers-as-strings.

(Also from https://softwareengineering.stackexchange. com/questions/49550/ which-hashing-algorithm-is-best-for-uniqueness-and-speed)

- Murmurhash seems to do well (and is fast), but has few guarantees.
- What do we do if we're OK with a slightly slower hash, but we REALLY want to be sure it does well?
- Answer: cryptographic hashes! Secure even for cryptographic applications; no known statistical weaknesses
- Examples: SHA-3, BLAKE2, many others
- Broken: MD5, SHA-1, many others

## **Modern Instructions and Intrinsics**

- Processors aren't getting much faster
- So: modern processors comes with tools that help you do common computations more quickly
- Let's talk about a few of these tools specifically
- Note: need to use lab computers for access to many of these
  - Most processors have some kind of equivalent tools, but I can only guarantee for Intel
  - Need the right kind of processor

```
unsigned int v;
unsigned int c = 32;
v &= -signed(v);
if (v) c--;
if (v & 0x0000FFFF) c -= 16;
if (v & 0x00FF00FF) c -= 8;
if (v & 0x0F0F0F0F) c -= 4;
if (v & 0x33333333) c -= 2;
if (v & 0x55555555) c -= 1;
```

- Count the number of zeroes at the beginning (or end) of a number
- Can do using a few bit tricks
- But nowadays...single CPU operation (usually)

## • Intrinsics!

- Library functions built into the compiler itself ( gcc in our case)
- Usually: will use the best compiler option if it exists; will do a very high-quality subroutine if not
  - For example: their version of manually counting the trailing zeroes will almost definitely be faster than your for loop
  - (And even a version using bit tricks)
  - And you don't need to worry about debugging it!

## Example intrinsic for counting zeroes

- int \_\_builtin\_ctzl (unsigned long)
- Note that you have to use a type like unsigned long (not uint64\_t)
- If you want to count leading zeroes in an int, use int \_\_builtin\_ctz (unsigned int x)
- Let's look at some code using this

#	<pre>simdtests.c:10:</pre>	printf("For %ld num t
	.loc 1 10 3 discr	iminator 3
	<pre>movq -8(%rbp),</pre>	% <b>rax</b>
	rep bsfl %eax,	% <b>edx</b> # _1, _2
	movq -8(%rbp),	% <b>rax</b> # x, tmp85

• Lots and lots of them

• Get num 1s, get parity of num 1s, reverse the bytes in the word, raise number to power

• Not always going to have a CPU instruction

• Generally you need to call these manually

• (The compiler doesn't know that you're calculating the number of trailing 0s; so it can't make that substitution)

## **SIMD** instructions

- Something we've only touched on briefly in this class: word-level parallelism
- Idea: we can do computations on 64 bit numbers very quickly (say 1 clock cycle)
- If our data is much less than 64 bits, can get extra computation done more quickly.

## World level parallelism example

- Can you test if a string (array of chars) starts with "abcd" in O(1) time?
  - Calculate a uint64\_t corresponding to the correct integer
  - Cast the string pointer to a uint64\_t pointer, then compare them
  - Watch for endianness!!!

- Words of 64 bits allow us to do lots of computations in one (or a few) clock cycles
- Example: taking the bitwise OR of two 64 bit numbers is basically doing 64 computations at once
- This is literally parallelism: the circuits in the chip do these operations simultaneously
- Hard to do things like add (almost impossible to multiply): why?
  - Carries (etc.) mess us up!
  - We'd have to leave "space" between pieces of data; lots of setup means it's probably not worth it

## One last fun(?) example

#### Reverse the bits in a byte with 4 operations (64-bit multiply, no division):

unsigned char b; // reverse this byte

b = ((b \* 0x80200802ULL) & 0x0884422110ULL) \* 0x0101010101ULL >> 32;

The following shows the flow of the bit values with the boolean variables a, b, c, d, e, f, g, and h, which comprise an 8-bit byte. Notice how the first multiply fans out the bit pattern to multiple copies, while the last multiply combines them in the fifth byte from the right.

abcd efgh (-> hgfe dcba) 4 0010 0000 0000 1000 0000 0010 (0x80200802) Oabc defg h00a bcde fgh0 Oabc defg h00a bcde fgh0 & 0000 1000 1000 0100 0100 0010 0010 0001 0001 0000 (0x0884422110) 0000 d000 h000 0c00 0q00 00b0 00f0 000a 000e 0000 0000 0001 0000 0001 0000 0001 0000 0001 0000 0001 (0x0101010101) 0000 d000 h000 0c00 0g00 00b0 00f0 000a 000e 0000 0000 d000 h000 0c00 0c00 00b0 00f0 000a 000e 0000 0000 d000 h000 0c00 0q00 00b0 00f0 000a 000e 0000 0000 d000 h000 0c00 0g00 00b0 00f0 000a 000e 0000 0000 d000 h000 0c00 0g00 00b0 00f0 000a 000e 0000 0000 d000 h000 dc00 hq00 dcb0 hqf0 dcba hqfe dcba hqfe 0cba 0qfe 00ba 00fe 000a 000e 0000 >> 32 0000 d000 h000 dc00 hq00 dcb0 hqf0 dcba hqfe dcba δ hafe dcba

Note that the last two steps can be combined on some processors because the registers can be accessed as bytes; just multiply so that a register stores the upper 32 bits of the result and the take the low byte. Thus, it may take only 6 operations.

## https://graphics.stanford.edu/~seander/bithacks.html# ReverseByteWith64Bits

- Good part: takes advantage of how computers are built to speed up computation
- Bad parts?
  - Only works for a few operations (can't even really add)
  - Only works on really small pieces of data

## Extending it forward

- Having fast operations on 64 bit data can speed up operations on 1-bit or 8-bit data
- ...but often we want to operate on 32 or 64 bit data. It would be nice if we could do the same!
- Honestly it'd be nice if we could do something better like adding and multiplying rather than just taking OR or doing weird string comparisons...
- This is the purpose of SIMD!



- SIMD: Single Instruction Multiple Data
- A single instruction does an identical operation to multiple pieces of data
- Specialized circuits operate on each piece of data individually
- Can do bitwise operations, adding, multiplying, some others
- Also some operations to help load and read data
- Introduced on Intel processors in 1999, but fairly significantly expanded recently

## **Other Names**



- Sometimes called "vector" instructions
- And/or referred to using instruction sets: SSE, AVX, AVX2, AVX-512 (these are extensions to x86).

- Dipping our toes into parallelism
- Uniprocessor kind of parallelism
- GPU computation uses similar ideas
  - Scaled up significantly (much more speedup potential)
  - More restricted

## SIMD on lab computers

```
(gdb) print $ymm0
$1 = {
v8_float=\{0,0,0,0,0,0,0,0\},\
v4_double={0,0,0,0},
v32_int8={0 <repeats 32
     times>},
v16_int16={0 <repeats 16
     times>},
v8_int32={0,0,0,0,0,0,0,0},
v4_int64={0,0,0,0},
v2_int128={0,0}
}
```

- We have SSE, AVX, AVX2 instruction sets (don't have AVX-512)
- 16 "YMM" registers; each 256 bits
- (Older processors may only have 128 bit "XMM" registers.)
- Need to include #include <immintrin.h> and compile with -mavx2

## **SIMD Examples**

• Lots of identical operations on a set of elements; these operations are costly

- Elements are in nicely-sized chunks
  - Can always used specialized code to handle other cases

Let's add two arrays of 8 32-bit integers with one SIMD operation

• simdtests.c

_mm256_set_epi32(B[7],	B[6], B[5],	B[4], B[3]	, B[2], B[1], B[0]);	;
# D.25654, b				
# a, tmp178				
# tmp178,A				
# b, tmp179				
# tmp179,B				
	_mm256_set_epi32(B[7], # D.25654, b # a, tmp178,A # b, tmp179 # tmp179,B	_mm256_set_epi32(B[7], B[6], B[5], # D.25654, b # a, tmp178 # tmp178,A # b, tmp179 # tmp179,B	_mm256_set_epi32(8[7], B[6], B[5], B[4], B[3], # D.25654, b # a, tmp178 # tmp178, _A # b, tmp179,B	_mm256_set_epi32(B[7], B[6], B[5], B[4], B[3], B[2], B[1], B[0]) # D.25654, b # a, tmp178 # tmp178, _A # b, tmp179,B



• Let's add one value (10) to an array.

• Do we need to declare a new array to do this?

 How much time does SIMD add (in total in our implementation) take compared to normal add?

• It's a bit faster

- Can do vector comparisons, but get a 256 bit vector out
- Need a way to make that vector into something useful for us. Let's look at the code.
- int \_mm256\_movemask\_epi8(\_mm256 arg): returns a 32 bit int where the *i*th bit of the int is the first bit in the *i*th byte of the argument arg

## **Optimization comparison?**

- What happens when we change to O3?
- Everything gets faster!
- In previous tests: for adding, normally suddenly outpaces SIMD; finding the 0 element doesn't
- Guesses as to why? ...Let's take a look at the assembly
  - gcc is vectorizing the operations by itself and doing it very slightly better

## **SIMD** Discussion

## Tradeoffs

What are some downsides of using an SIMD instruction?

- SIMD instructions may be a little slower on a per-operation basis (folklore is a factor of ≈ 2 even for the operation itself, but it seems modern implementations are much better)
- Cost to gather items in new location
- SIMD is not always faster

How much can we save using SIMD? Let's say we're using 256 bit registers, and operating on 32 bit data.

- Factor of 256/32 = 8 at absolute best
- Realistically is going to be quite a bit lower in practice

• Bear in mind Amdahl's law when considering SIMD

• Only worth using on the most costly operations, and only when they work very well with SIMD

- What's a problem we've seen this semester that is particularly suited for SIMD speedup?
  - Hint: I'm not referring to any of the assignment problems
- Matrix multiplication: lots of time doing multiplications on successive matrix elements
- (SIMD works for some other problems too; I just wanted to highlight this as one of the classic examples.)

- A lot of the examples we saw were super simple
- Can the compiler use these operations automatically?
- As we just saw: yes it can
  - --ftree-vectorize
  - --ftree-loop-vectorize (turned on with O3)
  - Lots of extra option to tune gcc parameters for how it vectorizes
- But, as always, only is going to work in "obvious" situations.

#### Automatic Vectorization Example



when compiling with -03.