CSCI 357: HW 5 (due 04/08/2025)

**Problem 1.** For each of these statements, circle whether they are  $\mathbf{T}$  (True) or  $\mathbf{F}$  (False). You **do not need to provide a justification** but to practice the concepts, try coming up with proof outlines for the True statements and counter-examples for the False statements.

- **T F** Stable matchings are **unique**—that is, there cannot be two different matchings  $M_1$  and  $M_2$  on the same instance that are both stable.
- **T F** It is only possible to achieve one of the two properties—stability or strategyproofness (for both sides)—in a stable matching market.
- **T F** Consider a job j with preference list  $P_j$  in a candidate-proposing DA algorithm. Suppose j reports  $P'_j$  and all other preferece lists  $P_{-j}$  are fixed. Then, then the stable matching M output when the input is  $(P'_j, P_{-j})$  might be unstable with respect to preferences  $(P_i, P_{-j})$ .
- **T F** Consider a job j with preference list  $P_j$  in a candidate-proposing DA algorithm. Suppose j is matched to candidate c in this matching. Consider a new preference list of j,  $P'_j$  which is the same as  $P_j$  but is cutoff at c: that is, j removes c and all candidates below c from the list. If we run the candidate-proposing DA algorithm on  $(P'_j, P_{-j})$  (keeping the preferences  $P_{-j}$  fixed), then j will be matched to a candidate  $c^*$  that they prefer over c.