Converting Derivation Trees to Abstract Syntax Trees ____

The tree produced during a parse of a sentence using a grammar is called a <u>derivation tree</u>. Derivation trees show every step of how we came to understand the structure of a sentence. Oftentimes, we don't need all of the information provided in a derivation. Indeed, sometimes the quantity of detail makes understanding a structure more difficult.

For this reason, we often use an alternative tree form when trying to understand a structure. An <u>abstract syntax tree</u>, or AST, gives us the essential structure of a parsed structure. Many students find ASTs difficult to understand at first, because the rules for converting a derivation tree to an AST vary from one language to another. Nevertheless, an AST always has the following properties:

- All of the interior nodes of an AST are operations.
- All of the leaf nodes of an AST are data.

Consider the lambda calculus expression $\lambda a.(ab)c$. Its derivation tree and corresponding AST are shown side-by-side.







Figure 2: Abstract syntax tree for $\lambda a.(ab)c$.

Lambda Calculus Conversion Rules

In Figure 1 we have a complete record of a parse using the class lambda grammar. Figure 2 is a more compact representation of the same sentence, a small tree that shows only operations and data. What gets discarded depends on the language being analyzed. In the lambda calculus, the only operations are abstraction (λ) and application (θ). Everything else is data.

With practice, you can derive an AST directly from a lambda expression. If you have trouble seeing how this might be done, start by producing a derivation tree, then try converting the tree into an AST using the rules below. When you are done, discard the topmost <expr>.

Figure 3: Variables, where α is a variable like x.











Figure 6: Application, where e_1 and e_2 are expressions.



Figure 7: Abstraction, where α is a variable like x and e is an expression.