

# Homework 3

Due Sunday, March 1 by 11:59pm

Handout 6  
CSCI 334: Spring 2020

## Turn-In Instructions

For this assignment, upload a PDF called `hw3.pdf`. You may use the  $\text{\LaTeX}$  starter template for the assignment which is in your repository.

Turn in your work using the Github repository assigned to you. The name of the Github repository will have the form `cs334hw3_<your user name>`. For example, my repository would be `cs334hw3_dbarowy`. You should have received an invite to commit in the repository in your email. If you did not receive this email, please contact me right away!

**Honor code:** You may collaborate with one or more people on this assignment, but you may not write code together. All submitted work must be your own original work. If you work with a partner, please submit a `collaborators.txt` file that includes their names.

This assignment is due on Sunday, March 1 by 11:59pm.

## Reading

1. **(Required)** “Introduction to the Lambda Calculus,” Parts 1 and 2 from the course packet.
2. **(Required)** “Grammars and Parse Trees” from the course packet.

## Problems

### Q1. (10 points) ..... Parse Tree

Draw the parse tree for the derivation of the expression “ $1 - 5 + 24$ ”. Is there another derivation for “ $1 - 5 + 24$ ”? If so, draw the other parse tree. Refer to the grammar on the bottom of page 77 of the course packet.

### Q2. (20 points) ..... Lambda Calculus Reduction

Use lambda calculus reductions to find a shorter expression for  $(\lambda x. \lambda y. xy)(\lambda x. xy)$ . Begin by renaming bound variables. You should do all possible reductions to get the shortest possible expression. Your reduction should be in the two-column format shown in the course packet.

What goes wrong if you do not rename bound variables? Perform a second reduction (in two-column format) that shows what happens when you fail to rename.

### Q3. (20 points) ..... Parsing and Precedence

Draw parse trees for the following expressions, assuming the grammar and precedence described in Example 4.2 (course packet, pp. 81–82):

- (a)  $1 + 1 * 1$
- (b)  $1 + 1 - 1$
- (c)  $1 - 1 + 1 - 1 * 1$ , if  $+$  is given higher precedence than  $-$ .

#### Q4. (30 points) ..... Symbolic Evaluation

The Python program fragment

```
def f(x):  
    return x + 4  
  
def g(y):  
    return 3 - y  
  
f(g(1))
```

can be written as the following lambda expression:

$$\left( \underbrace{(\lambda f. \lambda g. f \ (g \ 1))}_{\text{main}} \underbrace{(\lambda x. (+ \ x \ 4))}_f \right) \underbrace{(\lambda y. (- \ 3 \ y))}_g$$

Reduce the expression to a normal form in two different ways, as described below.

- (a) (5 points) Reduce the expression by choosing, at each step, the reduction that eliminates a  $\lambda$  as far to the *left* as possible.
- (b) (5 points) Reduce the expression by choosing, at each step, the reduction that eliminates a  $\lambda$  as far to the *right* as possible.
- (c) (5 points) In pure  $\lambda$ -calculus, the order of evaluation of subexpressions does not affect the value of an expression. However, that is not the case for a language with side effects like Python or Java.
  - i. Write a Python or Java *instance method* **f** and expressions **e1** and **e2** for which evaluating arguments left-to-right and right-to-left produces different results. (Hint: Recall that in Python/Java, an instance method may refer to variables declared outside of the scope of the function definition.)
  - ii. What evaluation order is used by Java or Python? (you choose the language you prefer)

#### Q5. (20 points) ..... Translation into Lambda Calculus

A programmer is having difficulty debugging the following Python program. In theory, on an “ideal” machine with infinite memory, this program would run forever. In practice, this program crashes because it runs out of memory, since extra space is required every time a function call is made.

```
def f(g):  
    g(g)  
  
f(f)
```

Explain the behavior of the program by translating the definition of **f** into lambda calculus and then reducing the application **f(f)**. Note that an equivalent program in a statically typed language like Java or ML would not compile.

#### Q6. (5 points) ..... Bonus: Lambda Reduction with Sugar

Lambda expressions can be made easier to understand by the use of “syntactic sugar.” Syntactic sugar is additional syntax that simplifies readability while leaving the meaning (semantics) of a language expression unchanged.

For example, here is a “sugared” lambda expression using some extra syntax known as a **let** declaration:

```
let foo =  $\lambda x. \lambda y. (+ \ x \ y)$  in  
foo 2 3
```

The above expression may be “desugared” by replacing each `let  $z = U$  in  $V$`  with `( $\lambda z. V$ )  $U$` . First, we identify  $z$ ,  $U$ , and  $V$ :

$$\begin{aligned} z &= \text{foo} \\ U &= \lambda x. \lambda y. (+\ x\ y) \\ V &= \text{foo}\ 2\ 3 \end{aligned}$$

which yields:

$$(\lambda \text{foo}. (\text{foo}\ 2\ 3)) (\lambda x. \lambda y. (+\ x\ y))$$

and after reducing this expression, the value 5.

(a) Desugar the following expression:

```
let compose =  $\lambda f. \lambda g. \lambda x. f(g\ x)$  in
let h =  $\lambda x. (+\ x\ x)$  in
((compose h) h) 3
```

(b) Simplify the desugared lambda expression using reduction. Briefly explain why the simplified expression is the answer you expected.

#### Q7. (0 points) ..... Optional Feedback

How fun was this assignment on a scale of 1 to 5? (where the number indicates the number of minutes in a cold shower).

Do you have any additional comments or feedback that you would like me to know?

Please supply your answer as a `feedback.txt` file.

#### Q8. (1 point) ..... Bonus

Do any of the readings (“Introduction to the Lambda Calculus” parts 1 and 2, and “Grammars and Parse Trees”) have any errors? One bonus point (up to a total of 100%) will be awarded for every verified problem that you find and report.

Submit as a text file called `errors.txt`.