

CSCI 331:  
Introduction to Computer Security

Lecture 6: Password Cracking, part 1

Instructor: Dan Barowy  
**Williams**

Topics

Lab 1

Crypto refresher

Password database attacks

Your to-dos

1. Reading response (Oechslin) **due Wed 9/29**.
  - a. How to read this: understand the **big idea**.
2. Project part 1 **due Sunday 10/3**.
3. Lab 2 **due Sunday 10/10**.

Office hours:

Tuesday 1:10-2:35pm (**TBL 301**)

Thursday 4-6pm (**TBL 301**)

## Lab 1

1. Labs should make you stretch, not be **hard**.
2. Calibration—**everybody** gets **1 extra late day**.
3. Extra office hours tonight: 6:30-7:30pm  
→ **TCL 312** ←
4. Feeling confused? This is **not bad**. Get in touch.
5. Feeling discouraged? This is **not good**. Get in touch.
6. Nobody who hands in **something** will do poorly in this class, because...
7. **Resubmissions**.

### Office hours:

Tuesday 1:10-2:35pm (**TBL 301**)

Thursday 4-6pm (**TBL 301**)

+

Tonight only 6:30-7:30pm (**TCL 312**)

## Cryptography refresher

**Encryption** is the **process of encoding a message** so that it can be read only by the sender and the **intended recipient**.

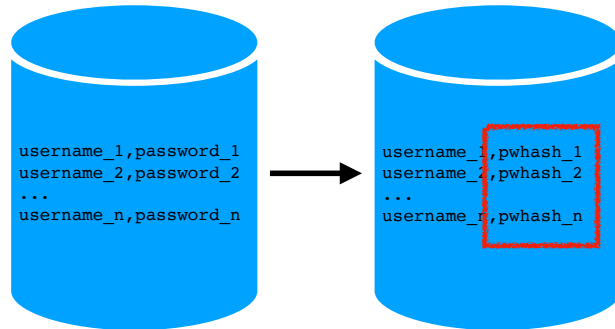
- A **plaintext**  $p$  is the original, unobfuscated data. This is information you want to protect.
- A **ciphertext**  $c$  is encoded, or encrypted, data.
- A **cipher**  $f$  is an algorithm that converts **plaintext** to **ciphertext**. We sometimes call this function an **encryption function**.
  - ✱ More formally, a cipher is a function from plaintext to ciphertext,  $f(p)=c$ . The properties of this function determine what kind of encryption scheme is being used.
- A **sender** is the person (or entity) who enciphers or encrypts a message, i.e., the party that converts the plaintext into ciphertext.  $f(p)=c$
- A **receiver** is the person (or entity) who decipheres or decrypts a message, i.e., the party that converts the ciphertext back into plaintext.  $f^{-1}(c)=p$

See the reading [Why Stolen Password Databases are a Problem](#) for a little more nuance.

## Lab 2

## Scenario

Entire password database **leaked** (bug; misconfiguration; theft by authorized personnel).



We keep passwords in **hashed** form.  
Hashes are **not invertible**.

## Password database attacks

- Random guessing attack
- Enumeration attack
- Dictionary attack
- Precomputed hash chain attack
- **Rainbow** table attack

## Random guessing



```
for each entry in database:
    not_found = true
    // try until found
    while not_found:
        // random plaintext
        p = randPassword()
        // create ciphertext
        c = hash(p)
        // compare
        if c = entry.pwhash:
            print entry.pwhash, p
            not_found = false
```

Complexity?

## Random guessing: complexity (one pw)



**m** = # of possible passwords

**p** = probability that random guess is correct

$$= 1/m$$

**X** = # guesses until success

$$E[X] = (1-p)/p \quad (\text{geometric dist})$$
$$= m - 1$$

$O(m)$  average **per pw**     $O(mn)$  average for **all pw**

## Wait a sec...

Suppose password is: `password`

Hashes to `5f4dcc3b5aa765d61d8327deb882cf99`

Suppose we guess: `b1d78hdd`

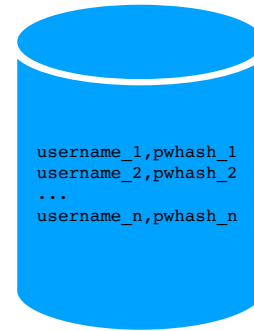
Hashes to `310fca1c70732a8191d0199bddba3a97`

Clearly that was not the passwd.

Does it make sense to guess: `b1d78hdd` again?

**No!** We should **remember** bad guesses.

## Enumeration: slightly better



for each entry in database:

```
i = 0
not_found = true
// try until found or out of pt
while not_found && i < NUM_PT:
    // gen ith possible plaintext
    p = genPassword(i)
    // create ciphertext
    c = hash(p)
    // compare
    if c = entry.pwhash:
        print entry.pwhash, p
        not_found = false
    i++
```

Complexity?

## Enumeration: complexity



$m$  = # of possible passwords

Average guesses to find **one pw**:

$$O(m/2)$$

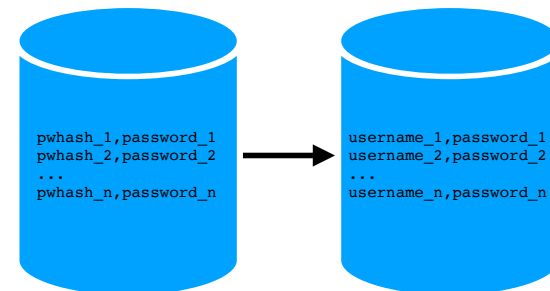
Average guesses to find **all pw**:

$$O(n \times m/2)$$

## Dictionary attack

A **dictionary attack** is a form of **brute force attack** technique for **recovering passphrases** by systematically **trying all likely possibilities**, such as words in a dictionary.

Critically, a dictionary attack only tries each possibility once. It **trades space for time**.



## Dictionary: much better

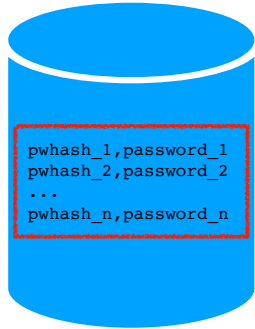
Ahead of time:

```
while i < NUM_PT:
    // gen ith possible plaintext
    p = genPassword(i)
    // create ciphertext
    c = hash(p)
    // save
    cracked_db[c] = p
```

Later:

```
for each entry in database:
    print cracked_db[entry.pwhash]
```

Complexity?



## Dictionary attack: complexity

**m** = # of possible passwords

Time to compute dictionary:

$O(m)$

Time to lookup **one pw**:

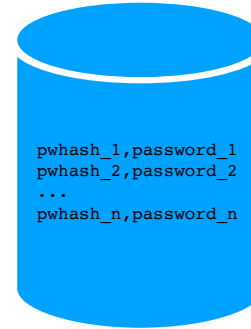
$O(\log m)$

Time to lookup **all pws**:

$O(n \log m)$

**Space** needed:

$O(m)$



## Activity: How much space?

It depends on the **number of possible passwords**.



Password scheme:

- Uppercase letters and numbers, except 0 and I.
- Up to 8 digits

**How many passwords are there?**

## Activity: How much **space**?

**m** = # of passwords

$$= \sum_{k=1}^8 34^k = 1\,839\,908\,871\,710$$

$\approx 1.8$  trillion passwords

Suppose per-pw storage is **always 16 bytes**.  
(8 bytes for ciphertext, 8 bytes for plaintext)

$16 \times (1.8 \times 10^{12})$  bytes

$\approx 29$  terabytes

Is this a **feasible attack**?

## Is this a feasible attack?

space:  $\approx 29$  terabytes

### Time?

Suppose I can generate 1 million pw/sec

$(1.8 \times 10^{12}) / 10^6 \approx (1.8 \times 10^6)$  seconds

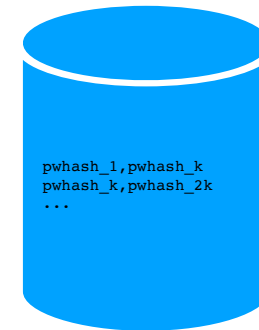
$\approx 21$  days with one computer.

This is **definitely feasible!**

## Precomputed hash chains

A **PCHC attack** is a form of **brute force attack** technique for **recovering passphrases** by systematically **trying all likely possibilities**, such as words in a dictionary.

Critically, a PCHC attack only tries each possibility once. It **trades space for time, but it compresses the database.**



## Hash function

Suppose we have:

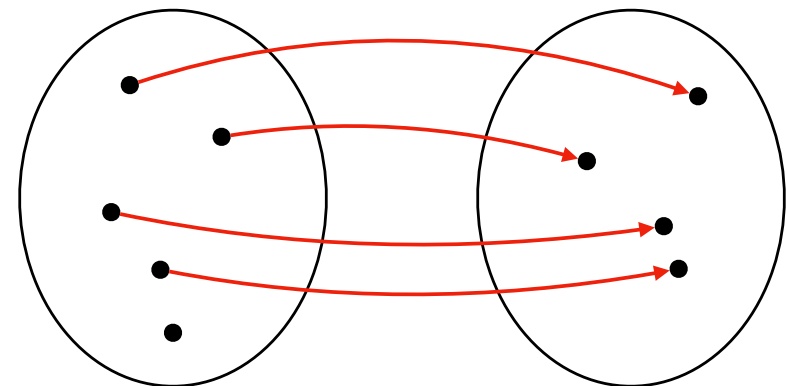
$f(p)=c$ , a **cipher** that maps **plaintexts** to **ciphertexts**; in this case, a **hash function**.

Because  $f$  is a hash function, there is **no inverse function** such that  $f^{-1}(f(p))=p$ .

## Hash function

Space of possible plaintexts

Space of possible hashes



8 digits, 0-9, a-f

64 digits, 0-9, a-f

→ hashing

plaintext: "9a55302d"

ciphertext: "4651f1799e5e36c878f3d980c59e94ae"

## Reducer function

Suppose we have:

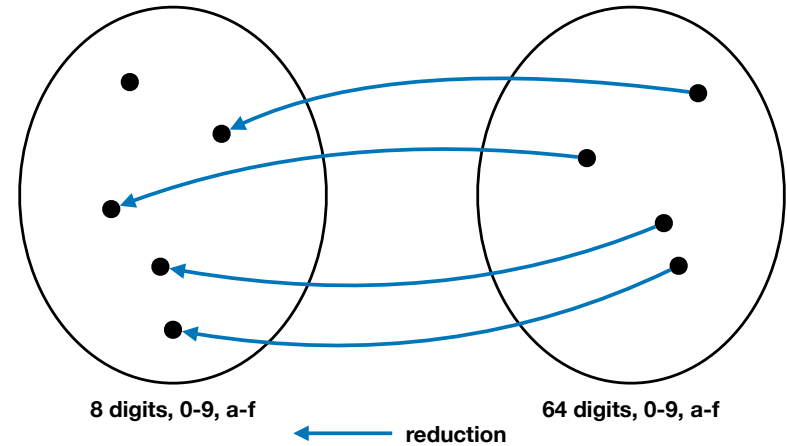
$r(c)=p$ , that maps **ciphertexts** to **plaintexts**, called a **reducer**.

A reducer is **not the inverse** of the hash!

## Reducer function

Space of possible plaintexts

Space of possible hashes



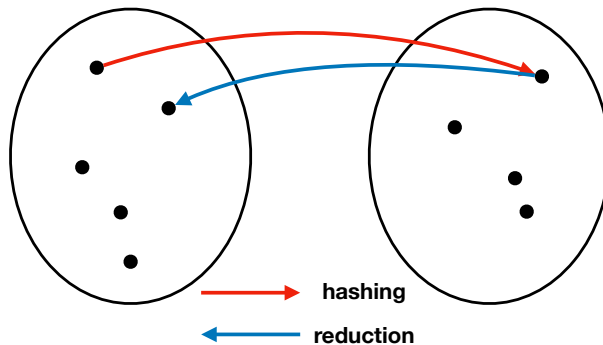
ciphertext: "4651f1799e5e36c878f3d980c59e94ae"

plaintext: "4651f179"

## Reducer function properties

A reducer  $r(c)=p$  only needs to satisfy a couple properties.

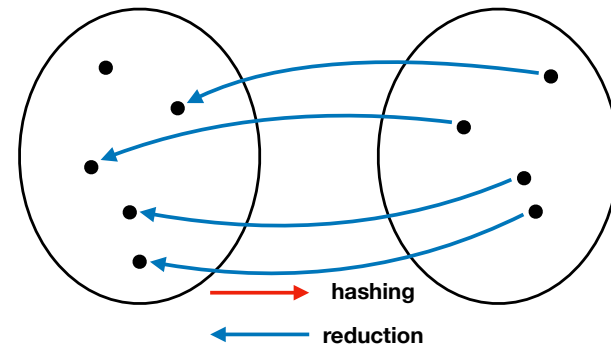
1. A reducer's output,  $p$ , should map to the same domain as the *input* of the hash function,  $f(p)=c$  (i.e., plaintexts)



## Reducer function properties

A reducer  $r(c)=p$  only needs to satisfy a couple properties.

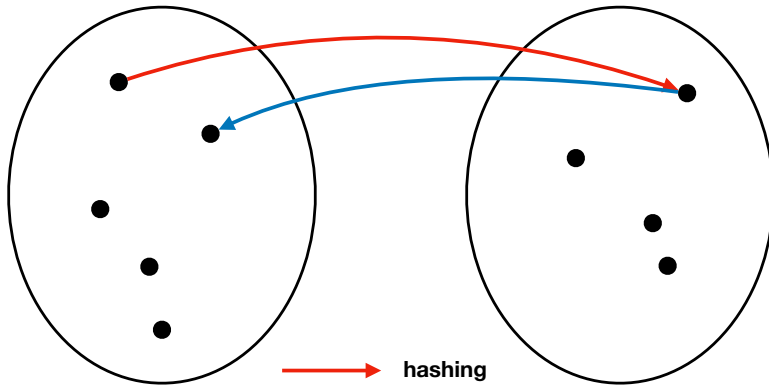
2. All plaintexts should be selected, given the space of ciphertexts, with equal probability.



## Hash-reduce “round trip”

Space of possible plaintexts

Space of possible hashes



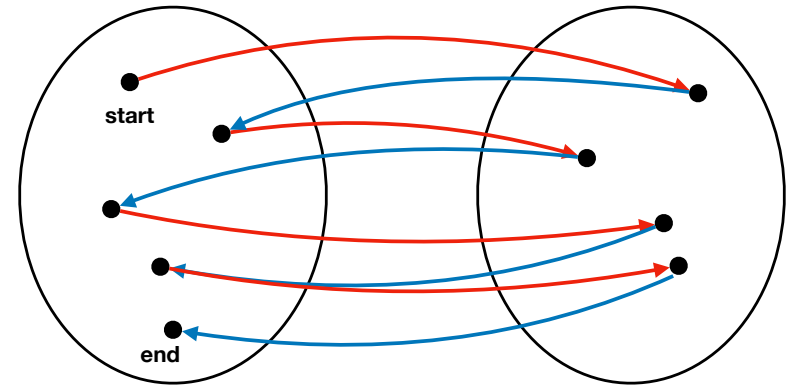
→ hashing  
← reduction

plaintext: “9a55302d”    ciphertext: “4651f1799e5e36c878f3d980c59e94ae”  
ciphertext: “4651f1799e5e36c878f3d980c59e94ae”    plaintext: “4651f179”

## Hash chain

Space of possible plaintexts

Space of possible hashes

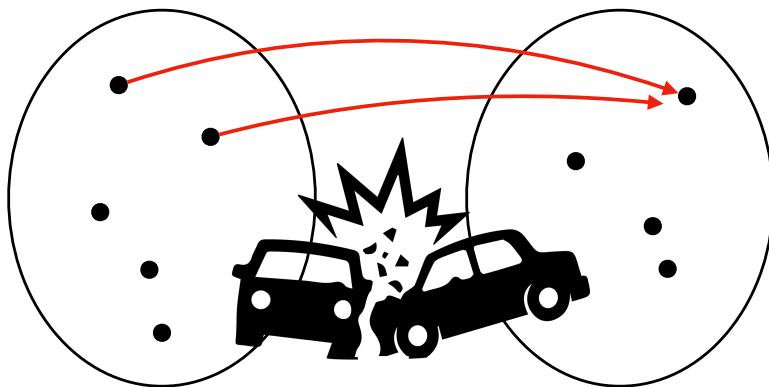


→ hashing  
← reduction

## Hash functions are not usually perfect

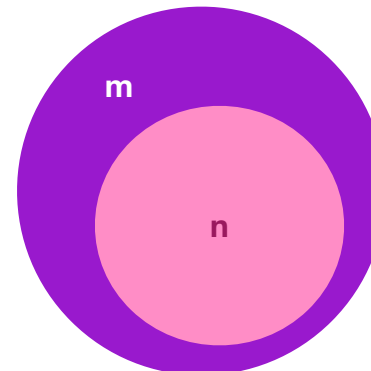
Space of possible plaintexts

Space of possible hashes



→ hashing  
**Collisions!**

## Hashes are guaranteed to collide



$m$ : # of passwords

$n$ : # of hashes

If  $m > n$ , we know that **at least**  $(m-n)/m$  must collide.

“pigeonhole principle”



## Thought experiment

Let's **suspend disbelief** for a moment.

1. Our **hash** function is **perfect**, chooses ciphertext with probability  $1/m$ .
2. Our **reducer** function is **perfect**, chooses plaintext with probability  $1/m$ .
3. The **combination** of hash function and reducer function is also **perfect**.

Real cryptographic hash functions are designed to approximate #1.

Real reducers can actually be perfect.

## Thought experiment

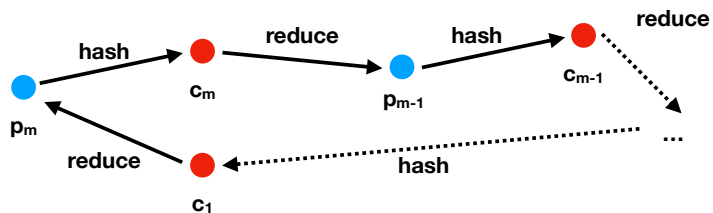
What can we **do** with this information?

## Thought experiment

- plaintexts
- ciphertexts

Suppose  $f(p_i) = c_i$

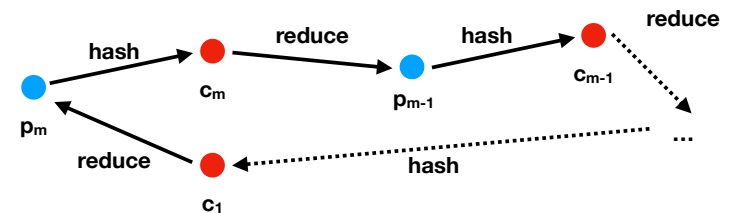
Suppose  $r(c_i) = p_{i-1}$  if  $i > 1$  otherwise  $p_m$



## Thought experiment

- plaintexts
- ciphertexts

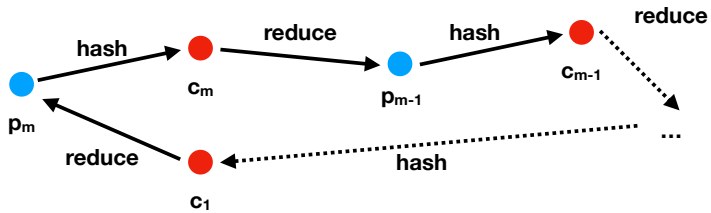
Such a scheme (a **hash chain**) lets us generate all plaintexts (and hashes) from a seed plaintext.



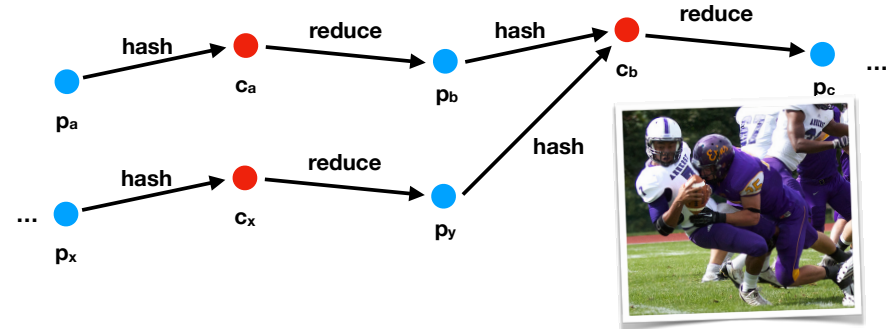
Only need to save the seed. **Drawbacks?**

## Thought experiment: **drawbacks**

- Saving just the first password **buys us nothing**. On average, we have to compute  $O(m/2)$  hash-reductions to find a password.
- **Hash functions collide!**



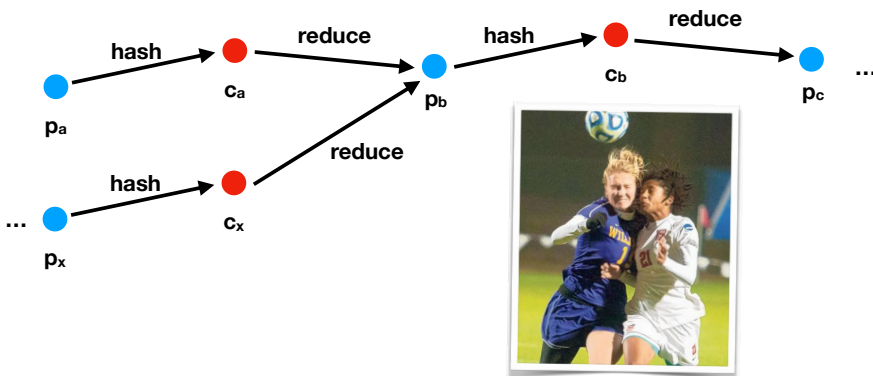
## Collisions in a hash chain



After the **collision**, the chain “**loops**.”

Collisions prevent us from enumerating the **entire space**!

## Collisions in a hash chain



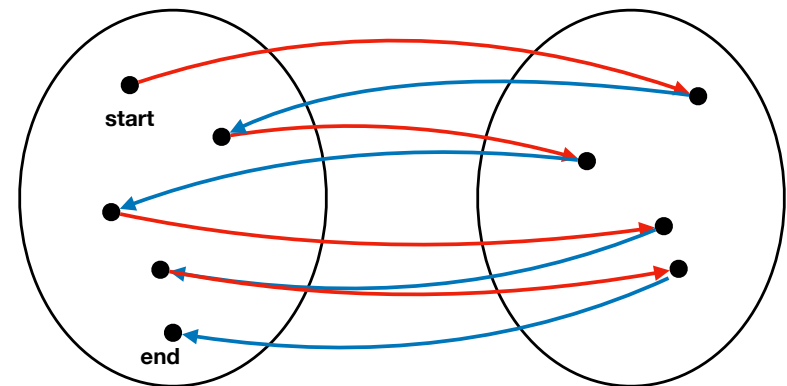
**Reducers** can produce collisions too!

This is what we mean by an **imperfect reducer**.

## Hash chain

Space of possible plaintexts

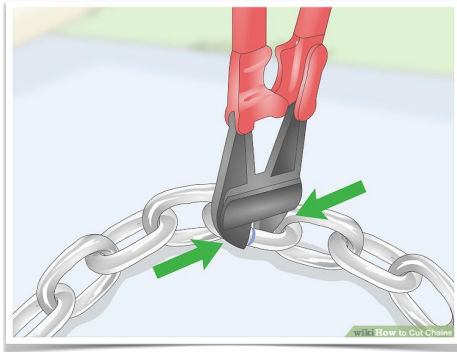
Space of possible hashes



→ hashing  
← reduction

# Hash chain of length k

We are going to chop up our long chain into **smaller chains** of length **k**.

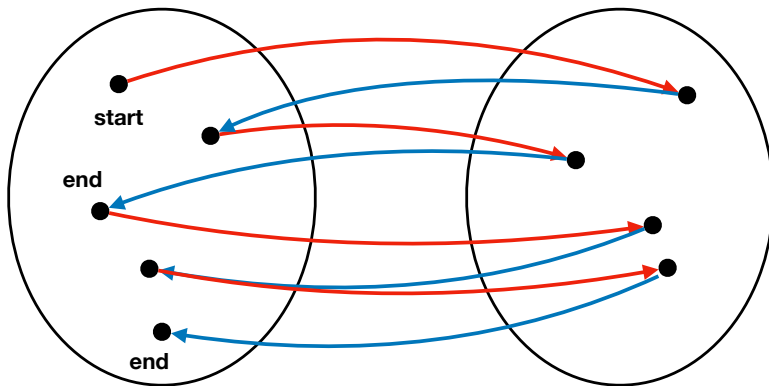


A screenshot of a wikiHow article titled "How to Deal With a Police Polygraph Test". The article is co-authored by Clinton M. Sandvick, JD, PhD, a former civil litigator. It includes a table of contents with sections like "Understanding the Test", "Preparing for the Test", "Taking the Test", "Questions &amp; Answers", "Related Articles", and "References". There is also a user comment from Neshia B. dated Mar 15, 2017, and a "Share yours!" button.

## Hash chain

Space of possible plaintexts

Space of possible hashes

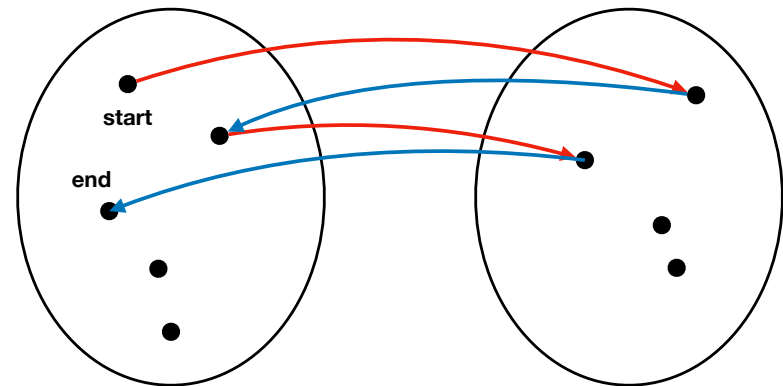


→ hashing  
← reduction

## Hash chain of length 2

Space of possible plaintexts

Space of possible hashes

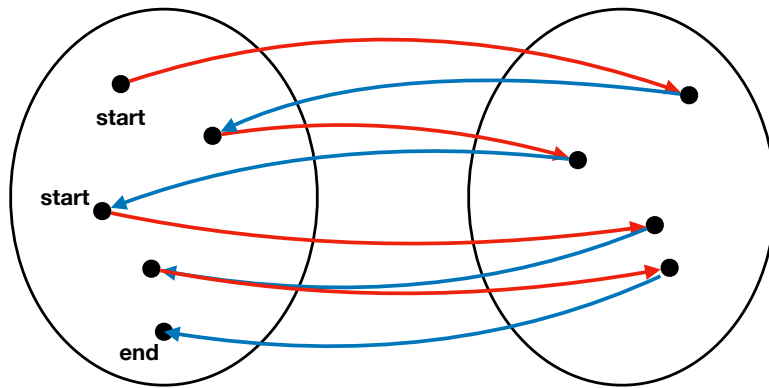


→ hashing  
← reduction

## Hash chain

Space of possible plaintexts

Space of possible hashes

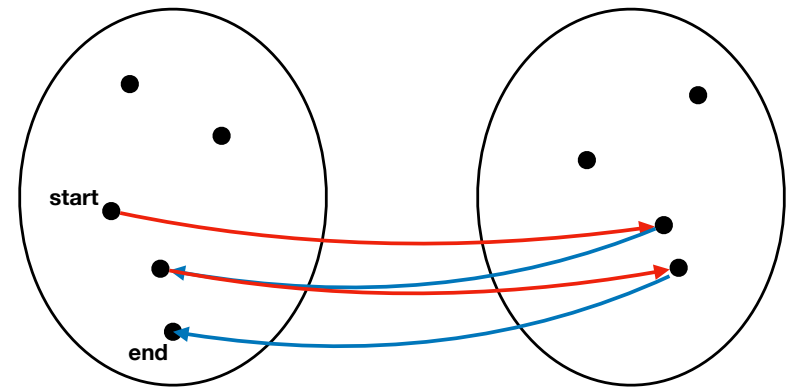


→ hashing  
← reduction

## Hash chain of length 2

Space of possible plaintexts

Space of possible hashes



→ hashing  
← reduction

## Store only **start** and **end**

start, end  
 $p_m$  ,  $p_{m-3}$   
 ...  
 $p_5$  ,  $p_3$   
 $p_3$  ,  $p_1$

## Store it **backward**

end, start  
 $p_{m-3}$  ,  $p_m$   
 ...  
 $p_3$  ,  $p_5$   
 $p_1$  ,  $p_3$

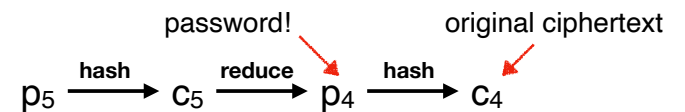
## Suppose you are given $c_4$

end, start  
 $p_{m-3}$  ,  $p_m$   
 ...  
 $p_3$  ,  $p_5$   
 $p_1$  ,  $p_3$

reduce  
 $c_4 \longrightarrow p_3$

Is  $p_3$  an **end point**? **yes**

**Hash** and **reduce** from **start point**.



## Recap & Next Class

### Today we learned:

Password attacks

Password attack complexity

Trading space for time

### Next class:

PCHC lookup algorithm