

**CSCI 136**  
**Data Structures &**  
**Advanced Programming**

**Spring 2020**

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# Administrative Details

- Lab 6: Two Towers
  - Lab handout has detailed instructions
  - Please Collaborate!
  - See lab-specific videos for more details

# Last Time

- Iterators
  - General purpose mechanism for traversals
- Iterator interface (Java)
- AbstractIterator class (structure5)
  - Adds get ( ) and reset ( )

# Today's Outline

- Brainstorm some “nifty” Iterators
- Bit operations
  - Useful for data structures in general, but
    - ...necessary for Lab 6
- `BIterator.java`: an iterator for enumerating the individual bits in the binary representation of an Integer

# Some “Nifty” Iterators

- Iterators aren’t limited to simply traversing the elements of a data structure
  - We can define arbitrary “traversals”
  - We can “generate” elements that are not stored anywhere in memory
- An iterator just gives us an interface that we can fill in however we want!

# ReverseIterator.java

- Goal:
  - Take an iterator `it` and return its values in the opposite order that it yields them
- Implementation:
  - Problem: Iterators progress in one direction only
    - `next()` but no `previous()`
  - Any ideas?

# Skiplterator.java

- Goal:
  - Take an iterator `it` and a value `val`
  - Return sequential values from `it` as long as they don't match `val`
- Implementation:
  - `next ( )` and `hasNext ( )`
    - Pre-calculate the values in preparation for the `next ( )` call
  - What if last value in `it` is equal to `val`?

# Biterator.java

- Goal:
  - Take a number  $n$ , and yield its bits (0 or 1) from least significant bit to most significant bit
- Implementation:
  - Think back to Lab 3
- We will revisit this at the end of lecture, after covering bit operations

# Representing Numbers

- Humans usually think of numbers in base 10
- But even though we write `int x = 23;` the computer stores `x` as a sequence of 1s and 0s

- Recall Lab 3:

```
public static String numInBinary(int n) {  
    if (n <= 1)  
        return "" + n%2;  
  
    return printInBinary(n/2) + n%2;  
}
```

- 00000000 00000000 00000000 00010111

# numInBinary(int n)

- What was our strategy for writing (recursive) `printInBinary` for Lab 3?
  - Use mod to isolate the least significant bit
  - Divide by 2 and recurse

```
public static String numInBinary(int n) {  
    if (n <= 1)  
        return "" + n%2;  
  
    return printInBinary(n/2) + n%2;  
}
```

# Bitwise Operations

- We can use *bitwise* operations to manipulate the 1s and 0s in the binary representation
  - Bitwise ‘and’: &
  - Bitwise ‘or’: |
- Also useful: bit shifts
  - Bit shift left: <<
  - Bit shift right: >>

# & and |

- Given two integers a and b, the *bitwise or* expression  $a | b$  returns an integer s.t.
  - At each bit position, the result has a 1 if that bit position had a 1 in **EITHER** a **OR** b
  - $3 | 6 = ?$        $011 | 110 = 111$
- Given two integers a and b, the *bitwise and* expression  $a \& b$  returns an integer s.t.
  - At each bit position, the result has a 1 if that bit position had a 1 in **BOTH** a **AND** b
  - $3 \& 6 = ?$        $011 \& 110 = 010$

# >> and <<

- Given two integers  $a$  and  $i$ , the expression  $(a \ll i)$  returns  $(a * 2^i)$ 
  - Why? It shifts all bits **left** by  $i$  positions
  - $1 \ll 4 = ?$      $00001 \ll 4 = 10000$
- Given two integers  $a$  and  $i$ , the expression  $(a \gg i)$  returns  $(a / 2^i)$ 
  - Why? It shifts all bits **right** by  $i$  positions
  - $1 \gg 4 = ?$      $00001 \gg 4 = 00000$
  - $97 \gg 3 = ?$      $(97 = 1100001)$   
 $1100001 \gg 3 = 1100$
- Be careful about shifting left and “overflow”!!!

# Revisiting numInBinary(int n)

- How would we rewrite a recursive numInBinary using bit shifts and bitwise operations?

```
public static String numInBinary(int n) {  
    if (n <= 1) // no non-zero digits  
        return "" + n;  
    return numInBinary(n >> 1) + (n & 1);  
}
```

# Revisiting numInBinary(int n)

- How would we write an **iterative** `printInBinary` using bit shifts and bitwise operations?

```
public static String printInBinary(int n,  
                                   int width) {  
    String result = "";  
    for(int i = 0; i < width; i++)  
        if ((n & (1<<i)) == 0)  
            result = 0 + result;  
        else  
            result = 1 + result;  
    return result;  
}
```

# BIterator.java

- Goal:
  - Take a number `n`, and yield its bits (0 or 1) from least significant bit to most significant bit
- Implementation:
  - Store `n`
  - Each `next ( )` isolates the LSB and shifts
  - `hasNext ( )?`
  - `reset ( )?`

# General Rules for Iterators

1. Understand order of data structure
2. **Always call hasNext() before calling next()!!!**
3. Use remove with caution!
4. Don't add to structure while iterating:  
see `TestIterator.java`

# Up Next

- Two Towers Lab
  - Use the bitwise representation of a Java Long to represent a “subset” of blocks
  - Iterate through all possible subsets of blocks to find the subset that optimizes the problem
    - Find the “most even” stacking