CSCI 136: Data Structures and Advanced Programming

Lecture 21

Ordered Vector / Numbers

Instructor: Dan Barowy

Williams

Topics

- Ordered Vector
- Integer representation

Your to-dos

1. Read **before Wed**: Bailey, Ch 14-14.1, 14.3
2. Quiz due **Sat by 6pm**

Announcements

- CS Colloquium this **Friday, Nov 4 @ 2:35pm in Wege Auditorium (TCL 123)**

Rachit Nigam (Cornell University)

Programming Support for Hardware Accelerators

Rachit Nigam is a visiting researcher in the PLSE group at University of Washington and a PhD candidate studying computer science at Cornell University.

He is a part of the CAPRA and PL@Cornell research groups and is advised by Adrian Sampson. His research (Dahlia, Calyx) is focused on building high-level programming models for designing hardware accelerators.

Recall: `OrderedStructure`

Nonetheless, we can **signal our intent** with an interface.

How would we write an `OrderedStructure` interface?

Do its elements need to have **any special property**? (i.e., how would we **compare** them?)

Let's think about how we might implement this.

(code)

`OrderedVector`

Let's think about implementing an `OrderedVector`.

(code)

Integer representation

The bits of an integer

An **integer** is represented in computer memory as a **sequence of bits**, each having a value of either **0** or **1**. This representation is called **binary**.

Binary is number system where each digit can take one of two values; i.e., the **base** of the system is **2**.

You are probably more familiar with the **base 10** number system, aka **decimal**.

Any integer can be represented in either system.

Java `int`

The `int` data type in Java has 32 bits.

00000000 00000000 00000000 00010111

is the number 23.

$$
\begin{aligned}
&(00000000000000000000000000010111)_2 \\
&= (0 \times 2^{31}) + (0 \times 2^{30}) + (0 \times 2^{29}) + (0 \times 2^{28}) \\
&+ (0 \times 2^{27}) + (0 \times 2^{26}) + (0 \times 2^{25}) + (0 \times 2^{24}) \\
&+ (0 \times 2^{23}) + (0 \times 2^{22}) + (0 \times 2^{21}) + (0 \times 2^{20}) \\
&+ (0 \times 2^{19}) + (0 \times 2^{18}) + (0 \times 2^{17}) + (0 \times 2^{16}) \\
&+ (0 \times 2^{15}) + (0 \times 2^{14}) + (0 \times 2^{13}) + (0 \times 2^{12}) \\
&+ (0 \times 2^{11}) + (0 \times 2^{10}) + (0 \times 2^{9}) + (0 \times 2^{8}) \\
&+ (0 \times 2^{7}) + (0 \times 2^{6}) + (0 \times 2^{5}) + (1 \times 2^{4}) \\
&+ (0 \times 2^{3}) + (1 \times 2^{2}) + (1 \times 2^{1}) + (1 \times 2^{0}) \\
&= (23)_{10}
\end{aligned}
$$

Bitwise Operations

We can use bitwise operations to manipulate the `1`s and `0`s in the binary representation

- Bitwise 'and': `&`
- Bitwise 'or': `|`

Also useful: bit shifts

- Bit shift left: `<<`
- Bit shift right: `>>`

& and |

Given two integers `a` and `b`, the bitwise or expression `a | b` returns an integer s.t.

- At each bit position, the result has a `1` if that bit position had a `1` in EITHER `a` OR `b`
  - `3 | 6 = ?`

`011 | 110 = 111`

Given two integers `a` and `b`, the bitwise and expression `a & b` returns an integer s.t.

- At each bit position, the result has a `1` if that bit position had a `1` in BOTH `a` AND `b`
  - `3 & 6 = ?`

`011 & 110 = 010`

>> and <<

Given two integers `a` and `i`, the expression `(a << i)` returns `(a * 2^i)`

- Why? It shifts all bits left by `i` positions
  - `1 << 4 = ?`

`00001 << 4 = 10000`

Given two integers `a` and `i`, the expression `(a >> i)` returns `(a / 2^i)`

- Why? It shifts all bits right by `i` positions
  - `1 >> 4 = ?`

`00001 >> 4 = 00000`

  - `97 >> 3 = ?`

`1100001 >> 3 = 1100`

Recap & Next Class

Today:

Binary search

Number representations

Next class:

Tree ADT